# Vidyavardhini's College of Engineering \& Technology, Vasai <br> Department of Computer Engineering <br> Academic Year 2020-21 

Sub: Discrete Mathematics (CSC303)
Year/Sem:- SE/ Sem III
Max. Marks: 50

| Q.No. | Questions | Mark <br> s |
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| 1 | Which of the following two sets are equal? <br> a) $A=\{1,2\}$ and $B=\{1\}$ <br> b) $A=\{1,2\}$ and $B=\{1,2,3\}$ <br> c) $A=\{1,2,3\}$ and $B=\{2,1,3\}$ <br> d) $A=\{1,2,4\}$ and $B=\{1,2,3\}$ | 2 |
| 2 | What is the Cartesian product of $A=\{1,2\}$ and $B=\{a, b\}$ ? <br> a) $\{(1, a),(1, b),(2, a),(b, b)\}$ <br> b) $\{(1,1),(2,2),(a, a),(b, b)\}$ <br> c) $\{(1, a),(2, a),(1, b),(2, b)\}$ <br> d) $\{(1,1),(a, a),(2, a),(1, b)\}$ | 2 |
| 3 | The compound propositions $p$ and $q$ are called logically equivalent if $\qquad$ is a tautology. <br> a) $p$ $\square$ q <br> b) $p \rightarrow q$ <br> c) $\neg(p \vee q)$ <br> d) $\neg p \vee \neg q$ | 2 |
| 4 | $p \rightarrow q$ is logically equivalent to $\qquad$ <br> a) $\neg p \vee \neg q$ <br> b) $p \vee \neg q$ <br> c) $\neg p \vee q$ <br> d) $\neg p \wedge q$ | 2 |
| 5 | $(p \rightarrow q) \wedge(p \rightarrow r)$ is logically equivalent to $\qquad$ <br> a) $p \rightarrow(q \wedge r)$ <br> b) $p \rightarrow(q \vee r)$ <br> c) $p \wedge(q \vee r)$ <br> d) $p \vee(q \wedge r)$ | 2 |
| 6 | $\neg(p \rightarrow q)$ is logically equivalent to $\qquad$ <br> a) $p \leftrightarrow \neg q$ <br> b) $\neg p ~ \Theta q$ | 2 |


|  | c) $\neg p \leftrightarrow \neg q$ <br> d) $\neg q$ $\Theta p$ |  |
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| 7 | $p \vee q$ is logically equivalent to $\qquad$ <br> a) $\neg q \rightarrow \neg p$ <br> b) $q \rightarrow p$ <br> c) $\neg p \rightarrow \neg q$ <br> d) $\neg p \rightarrow q$ | 2 |
| 8 | The binary relation $\{(1,1),(2,1),(2,2),(2,3),(2,4),(3,1),(3,2)\}$ on the set $\{1,2,3\}$ is $\qquad$ <br> a) reflective, symmetric and transitive <br> b) irreflexive, symmetric and transitive <br> c) neither reflective, nor irreflexive but transitive <br> d) irreflexive and antisymmetric | 2 |
| 9 | Consider the relation: $R^{\prime}(x, y)$ if and only if $x, y>0$ over the set of non-zero rational numbers, then $R^{\prime}$ is $\qquad$ <br> a) not equivalence relation <br> b) an equivalence relation <br> c) transitive and asymmetry relation <br> d) reflexive and antisymmetric relation | 2 |
| 10 | Let $S$ be a set of $n>0$ elements. Let be the number $B_{r}$ of binary relations on $S$ and let $B_{f}$ be the number of functions from $S$ to $S$. The expression for $B_{r}$ and $B_{f}$, in terms of $n$ should be $\qquad$ <br> a) $n^{2}$ and $2(n+1)^{2}$ <br> b) $n^{3}$ and $n^{(n+1)}$ <br> c) $n$ and $n^{(n+6)}$ <br> d) $2^{\left(n^{*}\right)}$ and $n^{n}$ | 2 |
| 11 | Consider the binary relation, $\mathrm{A}=\{(\mathrm{a}, \mathrm{b}) \mid \mathrm{b}=\mathrm{a}-1$ and $\mathrm{a}, \mathrm{b}$ belong to $\{1,2,3\}\}$. The reflexive transitive closure of $A$ is? <br> a) $\{(a, b) \mid a>=b$ and $a, b$ belong to $\{1,2,3\}\}$ <br> b) $\{(a, b) \mid a>b$ and $a, b$ belong to $\{1,2,3\}\}$ <br> c) $\{(\mathrm{a}, \mathrm{b}) \mid \mathrm{a}<=\mathrm{b}$ and a , b belong to $\{1,2,3\}\}$ <br> d) $\{(\mathrm{a}, \mathrm{b}) \mid \mathrm{a}=\mathrm{b}$ and $\mathrm{a}, \mathrm{b}$ belong to $\{1,2,3\}\}$ | 2 |
| 12 | A function is said to be $\qquad$ if and only if $f(a)=f(b)$ implies that $a=b$ for all $a$ and $b$ in the domain of $f$. <br> a) One-to-many <br> b) One-to-one <br> c) Many-to-many <br> d) Many-to-one | 2 |
| 13 | The inverse of function $f(x)=x^{3}+2$ is $\qquad$ <br> a) $f^{-1}(y)=(y-2)^{1 / 2}$ <br> b) $f^{-1}(y)=(y-2)^{1 / 3}$ <br> c) $f^{-1}(y)=(y)^{1 / 3}$ <br> d) $f^{-1}(y)=(y-2)$ | 2 |


| 14 | Let $f$ and $g$ be the function from the set of integers to itself, defined by $f(x)=2 x+1$ and $g(x)=3 x+4$. Then the composition of $f$ and $g$ is <br> a) $6 x+9$ <br> b) $6 x+7$ <br> c) $6 x+6$ <br> d) $6 x+8$ | 2 |
| :---: | :---: | :---: |
| 15 | How many even 4 digit whole numbers are there? <br> a) 1358 <br> b) 7250 <br> c) 4500 <br> d) 3600 | 2 |
| 16 | In a multiple-choice question paper of 15 questions, the answers can be A, B, C or D. The number of different ways of answering the question paper are $\qquad$ <br> a) $65536 \times 4^{7}$ <br> b) $194536 \times 4^{5}$ <br> c) $23650 \times 4^{9}$ <br> d) 11287435 | 2 |
| 17 | How many five-digit numbers can be made from the digits 1 to 7 if repetition is allowed? <br> a) 16807 <br> b) 54629 <br> c) 23467 <br> d) 32354 | 2 |
| 18 | In a 7-node directed cyclic graph, the number of Hamiltonian cycle is to be $\qquad$ <br> a) 728 <br> b) 450 <br> c) 360 <br> d) 260 | 2 |
| 19 | If each and every vertex in $G$ has degree at most 23 then $G$ can have a vertex colouring of $\qquad$ <br> a) 24 <br> b) 23 <br> c) 176 <br> d) 54 | 2 |
| 20 | If G is the forest with 54 vertices and 17 connected components, G has $\qquad$ total number of edges. <br> a) 38 <br> b) 37 <br> c) $17 / 54$ <br> d) $17 / 53$ | 2 |


| 21 | A non empty set A is termed as an algebraic structure <br> a) with respect to binary operation * <br> b) with respect to ternary operation ? <br> c) with respect to binary operation + <br> d) with respect to unary operation - | 2 |
| :---: | :---: | :---: |
| 22 | An algebraic structure $\qquad$ is called a semigroup. <br> a) ( $\mathrm{P}, *$ ) <br> b) $(\mathrm{Q},+$, *) <br> c) $(P,+)$ <br> d) $(+$, *) | 2 |
| 23 | A monoid is called a group if $\qquad$ <br> a) $(a * a)=a=(a+c)$ <br> b) $\left(a^{*} c\right)=(a+c)$ <br> c) $(a+c)=a$ <br> d) $\left(a^{*} c\right)=\left(c^{*} a\right)=e$ | 2 |
| 24 | A cyclic group is always $\qquad$ <br> a) abelian group <br> b) monoid <br> c) semigroup <br> d) subgroup | 2 |
| 25 | $\{1, i,-i,-1\}$ is $\qquad$ <br> a) semigroup <br> b) subgroup <br> c) cyclic group <br> d) abelian group | 2 |

